PROBABILITY, Philosophy, Logic, Mathematics. Every proposition considered in itself is true or false; but relative to us, it can be certain; we can perceive more or less the relations which can exist between two ideas, or the suitability of the one with the other, based on certain conditions which link them, & which, when they are all known to us, give us the certitude of that truth, or of that proposition; but if we know only a part of it, we have then only a simple probability, which has so much the more truth, as we are assured of a greater number of these conditions. These are they which form the degrees of probability, of which a correct estimate & an exact measure could make the height of sagacity & of prudence.

Geometers have judged that their calculus can serve to evaluate these degrees of probability, at least to a certain point, & they have had recourse to logic, or to the art of reasoning, in order to discover the principles of it & to establish the theory of it. They have regarded certitude as a whole, & the probabilities as the parts of this whole. Consequently the correct degree of probability of a proposition has been exactly known to them, when they have been able to say & prove that this probability is worth a half, a fourth, or a third of certitude. Often they are content to assume it; their calculus in itself is no less correct, & these expressions, which can appear a little bizarre, are no less meaningful. Some examples taken from games, from wagers or from assurances, will clarify them. We suppose that one just said to me that I have had in a lottery a lot of ten thousand livres, I doubt the truth of this news. Someone, who is present, asks me what sum I would wish to give in order that he insured it to me. I offer him the half, that which suggests that I regard the probability of this news, only as a half-certitude; but if I had offered only one thousand livres, this had been to say that I have nine times more reason to believe the truth than to not believe it. Now this would make the probability carry to nine degrees, in a manner that certitude having ten, it would lack only one in order to add one whole proof to the news.

In ordinary usage, we call probable\(^1\) that which has more than half-certitude, credible\(^2\), that which surpasses it considerably, & morally certain\(^3\), that which touches whole certitude. We speak here only of moral certitude, which nearly coincides with mathematical certitude, although it is not susceptible to the same proofs. Moral evidence is therefore properly only a probability so great, that it is of a wise man to think and to act, in the case where one has this certitude, as one must think & act, if one had a mathematical one. It is

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\(^1\)Translator's note: The French word is probable.  
\(^2\)Translator's note: The French word is vraisemblable. This could be rendered as possible, but I have preferred here the word credible.  
\(^3\)Translator's note: The French phrase is moralement certain.
of a moral certitude that there is a city of Rome; the contrary implies no contradiction; it is not impossible that all those who say to me to have seen it, do not agree to be mistaken, that the books which speak of it are not done on purpose for this, that the monuments which we have of it, are not supposed; however, if I would refuse to render to me to an evidence supported on the proofs that I have of the evidence of Rome, simply because they are not susceptibles of mathematical demonstration, one would treat me, with reason, of insanity, because the probability that there is a city of Rome, so strongly surpasses over the suspicion that it can not be there at all, that at pain would one express by number this difference or the value of this probability. This example suffices to demonstrate the moral evidence & its degrees which are so much probabilities. A half-certitude forms the uncertain properly said, where the mind finding on all sides equal reasons, does not make what judgment to carry, what part to take. In this state of equilibrium, the smallest proof to us determines; frequently we seek it where there is neither reason nor wisdom to seek it; & as it is rather difficult in many cases, where the opposite reasons approach nearly to equality, to determine what are those which must surpass it, the wisest men extend the point of uncertainty; they do not fix it only at this state of the soul, where it is equally driven on all sides by the weight of the reasons; but they carry it yet onto each situation which approaches it sufficiently in order that we can not perceive inequality; it happens thence that the land of uncertainty is more or less vast, according to the degree more or less of knowledge, of logic & of courage. It is more compact to those who are the wisest or least wise; because temerity confines it more than prudence, by the hardiest of their decisions. Under this half-certitude or uncertainty, they find suspicion and doubt, which terminate at the certitude of falsity of a proposition. A thing is false of a moral evidence, when the probability of its existence is so much inferior to the contrary probability, that it has ten thousand, one hundred thousand odds against one that it is not.

Here are the degrees of probability between the two opposed evidences. Before researching the sources of them, it will not be useless in an article where we do not wish to content ourselves of simple geometric calculus, to establish some general rules, which are regularly observed by wise & prudent persons.

1° It is contrary to reason to seek probabilities, & to content ourselves of them there where we can attain evidence. One would scoff at a mathematician, who, in order to prove a proposition of geometry, would have recourse to some opinions, to some credibles, when he could bring its demonstration; or at a judge who would prefer to divine by the past life of a criminal, if he is culpable, rather than to hear his confession, by which he avows his crime.

2° It does not suffice to examine one or two of the proofs which one can put forward of it, it is necessary to weigh in the balance to examine all those which can come to our knowledge, & to serve to discover the truth. If we demand what probability there is that a man aged 50 years dies in the year, it does not suffice to consider that in general of one hundred persons of 50 years, there die of them around 3 or 4 in a year, & to conclude that there are odds 96 against 4, or 24 against one; it is necessary further to pay attention to the temperament of this man there, to the actual state of his sanity, to his kind of life, to his profession, to the country which he inhabits; each so many circumstances which influence on the duration of his life.

2° There are not enough proofs which serve to establish a truth, it is still necessary to examine those which combat it. One demands if a person known & absent from his country since 25 years, of whom one has had no news, must be regarded as dead? On one side one says that, in spite of all sorts of researches one has learned nothing of him; that as voyager
he could have been exposed to a thousand dangers, that a malady could have removed him in a place where he was unknown; that if he were alive, he would not neglect to give news of him, especially before presuming that he would have an inheritance to collect, & other reasons that we can allege. But, in these considerations, one opposes some others which must not be neglected. One says that the one of whom there is question is an indolent man, who, on other occasions has not written at all, that perhaps his letters are lost, that it can be impossible to write. This which suffices to show that in all things it is necessary to weigh the proofs, the probabilities on all sides, to oppose them the ones to the others, because a very probable proposition can be false, & that makes of it probability, there is none of them at all so strong that it can not be fought by a contrary yet stronger. Thence the opposition that one sees every day among the judgments of men. Thence most of the disputes which would end soon, if one wanted to not regard as evident that which is only probable, to listen & to weigh the reasons that one opposes our opinion.

4° Is it necessary to caution that in our judgments, it is prudent to give consent to any proposition only in proportion to its degree of credibility? Who would observe this general rule, would have all the rightness of mind, all the prudence, all the wisdom possible. But that we are quite alienated from it! The most common minds can, with some attention, discern the true from the false; others who have more penetration, know how to distinguish the probable from the uncertain or from the doubtful; but there are only the geniuses distinguished by their wisdom who can assign to each proposition its correct degree of credibility, & to proportion their opinion: ah but these geniuses are rare!

5° Moreover, the wise & prudent man will not consider only the probability of success, he will weigh still the grandeur of good or of ill that one must attend by taking such part of it, or determining for the contrary of it, or by remaining in inaction; he will prefer even the one where he knows that the appearance of success is quite slight, when he sees at the same time that the risk that he incurs is nothing or a quite small thing; & that to the contrary, if he succeeds, he can obtain a quite considerable wealth.

6° Since it is not possible to fix, with that precision what would be desired, the degrees of probability, we content ourselves of very nearly what we can obtain. Sometimes, by a delicateness badly understood, one is exposes oneself, & society, to some worse evils than those that one would wish to avoid; it is an art to know how to be alienated from perfection in certain articles, in order to approach disadvantage in some others more essential & more interesting.

7° Finally it seems useless to add here that in uncertainty we must suspend decision & acting until we have more knowledge, but that if the case is such that it permits no delay, it is necessary to stop at that which will appear most probable; & a time the decision that we have judged the most wise being taken, it is not necessary to repent it, even though the event would correspond in nothing to that which we had good reason to expect. If, in a fire, we can escape only by jumping through a window, it is necessary to determine for this decision, however injurious that it is. Uncertainty would be worse still, & whatever be the issue of it, we have taken the wisest decision, it is not at all necessary to have regret.

After these general rules of which it will be easy to make application, we come to the sources of probability. We reduce them to two kinds: the one contains the probabilities drawn from the consideration of the same nature, & of the number of causes or of the reasons which can influence on the truth of the proposition of which there is question: the other is founded only on past experience which can make us draw with confidence some conjectures for the future, when at least that we are assured that the same causes which have produced the past still exist, & are ascribed to produce the future.
An example will make better understood the nature and the difference of these two sources of probability. I suppose that one knows that one has placed into an urn thirty thousand tickets, among which there are ten thousand blacks & twenty thousand whites, & that one demands what is the probability that by drawing one from it at random, it will bring forth white? I say that by the sole consideration of the nature of things, & by comparing the number of causes which can make a white ticket come forth with the number of those which can make a black come forth, by that alone it is two times more probable that it will bring forth a white ticket than a black: so as the ticket which just came forth, is necessarily either black or white, if one dividing this certitude into three degrees or equal parts, one will say that there are two degrees of probability to draw a white ticket, & one degree for the black ticket, or that the probability of a white ticket is \( \frac{2}{3} \) of certitude, & that of the black ticket \( \frac{1}{3} \) of this certitude.

But, we suppose that I see in the urn only a great number of tickets, without knowing the proportion there is of the white to the blacks, or even without knowing if there is none at all of a third color, in this case, how to determine the probability to draw a white from it? I say that this will be by making some tests, that is to say, by drawing a ticket in order to see what it will be, then returning it into the urn, by drawing a second which I return also, then a third, a fourth, & so forth as many as I would wish. It is clear that the first ticket drawn being come up white, gives only a very slight probability that the number of whites surpasses that of the blacks, a second white drawn would increase this probability, a third would fortify it. Finally, if I drew from it in sequence a great number of whites, I will be right to conclude that they are all whites, & that with so much more credibility as I would have more tickets drawn. But, if on the first three tickets, I draw from it two whites & one black, I then say that there is some probability quite slight, that there are two times more whites than blacks. If, out of ten tickets, there are drawn four whites & six blacks, the probability increases, & it will increase in measure as the number of tests or of experiences will confirm to me always the same proportion of whites to the blacks. If I would have three thousand tests, & if I had two thousand white tickets against one thousand black, it would be nearly that the probability of drawing a white is the double of that of drawing a black.

This manner to determine probably the ratio of the causes which give birth to an event, to those which make it fail, or more generally the proportion of the reasons or conditions which establish the truth of a proposition with those which give the contrary, is applied to all that which can happen or not happen, to all that which can be or not be. When I see on the death registers, that during twenty, fifty years, or one hundred years, of the number of infants who are born, there die the third of them before the age of six years, I will conclude of a newly born infant, that the probability that he will attain at least the age of six years, is the \( \frac{2}{3} \) of certitude. If I see that of two players who play with equal marbles, the first wins always two matches, while the other wins only one, I will conclude with much probability that he is two times stronger than his antagonist; if I notice that some one of one hundred times that he has spoken to me, he has lied to me on ten occasions, the probability of his testimony will be in my mind only the \( \frac{9}{10} \) of certitude or even less.

The attention given in the past, the fidelity of the memory to retain that which has arrived & the exactitude of the registers to preserve events, make that which we call in the world, experience. A man who has experience is the one who having seen much & reflected much, can say to you very nearly (because here there is no mathematical precision) what probability there is that such event having arrived, such other will follow it; thus all things
equal besides, the more one has made of proofs or experiences, & the more one is assured of the precise ratio of the number of the favorable causes to the number of contrary causes.

One could demand if this probability increasing to infinity by a sequence of repeated experiments, can become in the end a moral certainty; or if these increases are so limited, that diminishing gradually, they make at infinity only a finite probability. Because we know that they have some increases which, although perpetual, make nonetheless at infinity only a finite sum; for example, if the first experience would give a probability which is only $\frac{1}{3}$ of certitude, & the second a probability which is only the third of this third, & the third a probability which is only the third of the second, & the fourth a probability which is only the third of the third, & thus to infinity. It would be easy, by the calculus, to see that all these probabilities together are only a half-certitude, so that one would have made in vain an infinity of experiences, one would never come to a probability which is confounded with moral certitude, that which would be concluding that experience is useless, & that the past proves nothing for the future.

Mr. Bernoulli, the geometer who understood best these sorts of calculations, has offered the objection & has given the response to it. One will find it in his book de arte conjectandi p. 4, in all its extent; a problem, according to him, as difficult as the quadrature of the circle. There he shows that the probability which was born from repeated experience, always increased, & increased so, that it approached indefinitely to certitude. His calculus teaches us to determine (the question proposed in a fixed manner) how many times it would be necessary to reiterate the experience in order to arrive to an assigned degree of probability. Thus, in the case of an urn full of a great number of white & black balls, one wishes to be assured by experience of the ratio of the whites to the blacks; Mr. Bernoulli finds that in order that it is one thousand times more probable that there are two blacks out of three whites as not every other supposition, it is necessary to have drawn from the urn 25,550 balls, & that, in order that this be two thousand times more probable, it was necessary to have made 31258 tests, finally, in order that this became seven thousand times more probable, it was necessary 36966 drawings. The difficulty & the length of the calculation do not permit the reporting here in entirety, one can see it in the book cited.

Thence it is demonstrated that the experience of the past is a principle of probability for the future; that we have good reason to expect some events conformed to those which we have seen arrive frequently, & moreover we have good reason to expect them anew. This principle received, one senses of what utility they would be in the questions of Physics, of Politics, & even in that which regards the common life, some exact tables which would fix, on a long sequence of events, the proportion of those which arrive in a certain fashion to those who arrive otherwise. The usages which one has drawn of the baptismal and mortuary registers are so great, that one should engage not only to perfecting them by noting, for example, the age, the condition, the temperament, the kind of death, &c. but also to make there of many other events, which one says very improperly to be the effect of chance; it is thus that one can form some tables which would note how many fires arrive in a certain time, how many epidemics of maladies are felt in certain periods of time, how many ships perish, &c. this which would be very convenient to resolve an infinity of useful questions, & would give to the attentive young people all the experience of the old men.

It is quite understood that one will not give into the abuse, which is only too ordinary, to the proof of experience, that one will not establish on a small number of facts a grand probability, that we will not go so far as to oppose or to prefer even a feeble probability to a contrary certitude, that we will not give into the foibles of those players who take only the cards which have won or those which have lost, although it is evident, by the nature
of the games of chance, that the preceding trials influence not at all on the following. Superstition however rightly more pardonable than so many of the others, which, on the slightest experience or on the least consequent reasoning, is introduced only too much into the flow of life.

To these two general principles of probability, we can join more particulars, such as the equal possibility of many events, the knowledge of causes, testimony, analogy & hypotheses.

1° When we are assured that a certain thing can happen only in a certain determined number of ways, & that we know or suppose that all these ways have an equal possibility, we can say with assurance that the probability, that it will happen in such fashion, is worth so much, or is equal to so many parts of certitude. I know, for example, that by casting a die at random, I bring forth surely either 1 point, or 2, 3, or 4, or 5, or 6. We suppose besides the die perfectly true, the possibility is the same for all the points. There are therefore here six equal probabilities, which altogether make certitude; thus, each is a sixth part of this certitude. This principle, entirely simple as it appears, is infinitely fecund; it is on it that are formed all the calculations which one has made & which one can make on the games of chance, on lotteries, on assurances, & in general on all the probabilities susceptible of calculation. There is question only of a grand patience & of a detail of combinations, in order to untangle the number of favorable events & the number of contraries. It is on this principle, joined to experience, that one determines the probabilities of human life, or of the times that a person of a certain age can probably be flattered with expectations of life; that which makes the foundation of the calculus of values of old age pensions, of tontines. See the essays on the probabilities of human life, & the works cited at the end of this article. It is extended to the calculation of the pensions put on two or three heads payables to the last living, on possessions, ration pensions, on assurance contracts, wagers, &c.

I have said that this principle was employed when we suppose the divers cases equally possible. And indeed, it is only by assumption relative to our limited knowledge, that we say, for example, that all the points of a die can come equally: this is not when they roll in the dice box, the one which itself must present, has already the disposition which, combined with that of the dice box, of the mat, or of the force & of the manner with which one casts the die, must make it surely to arrive; but all this being entirely unknown to us, we have no reason to prefer one point to another; we suppose them therefore all equally facile to arrive. However there can often be error in this assumption. If we wished to seek the probability to bring forth 8 points with two dice, it would make a greater fallacy, so to reason thus: with two dice, I can bring forth either 2, or 3, or 4, or 5, or 6, or 7, or 8, or 9, or 10, or 11, or 12 points; therefore the probability to bring forth 8, will be \( \frac{1}{11} \) of certitude; because it would be supposed that these 11 points are equally easy to bring forth, this which is not true. The most simple calculus of the game of tric-trac teaches us that out of 36 equally possible outcomes with two dice, 5 give us the point of 8; the probability will be therefore of 5 out of 36, or \( \frac{5}{36} \) of certitude, & not \( \frac{1}{11} \).

This fallacy is avoided easily in the calculus of games, where it is easy to determine the equal or unequal possibility of events; but it is more hidden, & it is only too common in the more composite cases. Thus, many people complain to be quite unhappy, because they have not been able to obtain certain happiness which is fallen in part to some others; they suppose that it was equally possible, equally proper, that this wealth arrived to them, without wishing to consider that they were not in a position so advantageous, which they had for them only a favorable manner, while the others had many of them, so that it would have been a great happiness that this sole way took place, without saying that the events
which they attribute to chance, are directed by an infinitely wise providence, who has all calculations, & who, by some reasons unknown to us, disposes some things in a manner much more appropriate than is the arrangement only our feeble knowledge or our passions would wish to put them.

After simple probability comes a composite probability which depends again on the same principle. This is the probability of an event which can happen only in the case that another event, itself simply probable, arrives. An example goes to explain it. I suppose that in a game of quadrille of 40 cards, one demands of me to draw a heart, the probability of succeeding is $\frac{1}{4}$ of certainty, because, there are 4 colors & 10 cards of each color equally possible. But if one says to me next that I will win if I bring forth the king of hearts, then the probability becomes composite; because $1^o$ it is necessary to draw a heart, & the probability if $\frac{1}{4}$; $2^o$ supposing that I have drawn a heart, the probability will be $\frac{1}{10}$, because there are 9 other hearts that I can also rightly draw than the king. This probability enters on the first, only the tenth of a quarter, or the $\frac{1}{40}$ of certitude. And it is clear, that since out of 40 cards I must draw precisely the king of hearts, I have of favorable only one case out of 40 equally possibles, or one against 39.

This composite probability is estimated therefore by taking from the first a part, such that one could take it away from entire certainty, if this probability was converted to certitude. A friend is departed for the Indies, in a fleet of twelve vessels, I understand that three of them have perished, & that the third of the crew of the rescued vessels is dead in the voyage; the probability that my friend is on one of the vessels arrived to a good port is $\frac{9}{12}$, & the one that he is not of the third dead en route, is $\frac{2}{3}$. The composite probability that he is yet alive, will be therefore $\frac{2}{3}$ of $\frac{9}{12}$ or $\frac{6}{12}$ or a half certitude. He is therefore for me between alive & dead.

We can apply this calculus to all sorts of proofs or reasonings, reduced for more clarity to the form prescribed by the art of reasoning: if one of the premises is certain, & the other probable, the conclusion will be the same degree of probability as this premise; but if the one & the other are simply probables, the conclusion will be only a probability of a probability, which is measured by taking from the probability of the major, a part such that expresses the fraction, which measures the probability of the minor. In these last examples the $\frac{9}{12}$ of $\frac{2}{3}$, which is the probability of the major, & the value of the conclusion will be $\frac{6}{12}$ or $\frac{1}{2}$.

Whence it would appear that the probability of the probability makes only a very slight probability. What will be therefore a probability of the third or fourth degree? or what to think of those reasonings so frequent, of which the conclusion is based only on many probable propositions which must each be true in order that the conclusion be also? but if it sufficed that one alone of among them took place in order to verify the conclusion, it would be entirely the contrary; the more we stack the probabilities, the more the thing would become probable. If, for example, someone said to me, I give to you a louis if you bring forth with two dice 8 points, the probability of bringing forth 8 is $\frac{5}{36}$; if he added, I give to you yet if you bring forth 6: then in order to win, it suffices to bring forth one or the other, my probability will be $\frac{5}{36}$ & $\frac{5}{36}$, that is to say, $\frac{10}{36}$, that which increases my expectation to win.

Here are the elements on which we can determine all the questions, & the examples depending on this first principle of probability.

$2^o$ We pass to the second, which is the knowledge of the causes & of the signs, which we can regard as some causes or some occasional effects. We say only one word particular to the probabilities, referring for the rest to the article CAUSE. There are some causes of
which the existence is certain, but of which the effect is only doubtful or probable; there
are some others of which the effect is certain, but of which the existence is doubtful; there
can be of them finally, of which the existence & the effect have only a simple probability.
This distinction is necessary; an example will explain it. A friend has responded not at
all to my letter; I seek the cause of it, there occur three of them: he is lazy, perhaps he is
dead, or his affairs have prevented him from responding to me. He is lazy, first cause of
which the existence is certain: I know that he writes with much difficulty; but the effect of
this cause is uncertain, because a lazy man is determined sometimes to write. He is dead,
second cause very uncertain, but of which the effect would be quite certain. He has some
affairs, third cause uncertain in itself: I suspect only that he has many affairs, & of which
the existence even supposed, the effect would be still uncertain, because one can have some
affairs & find however the time to write.

The same thing must apply to the signs; their existence can be doubtful, their signifi-
cation uncertain; & the existence & the signification can have only the credible. The
barometer descends, this is a sign of rain of which the existence is certain, but of which the
signification is doubtful: the barometer descends often without rain.

From this distinction it follows that the conclusion drawn from a cause or from a sign of
which the existence is certain, has the same degree of probability as is found in the effect
of this cause, or in the signification of this sign. We have only to reduce the example of
the barometer to this form. If the barometer descends, we will have rain: this is only prob-
able; but the barometer descends, this is certain: therefore we will have rain; conclusion
probable, of which experience gives the value. Likewise if the existence of the cause or of
the sign is doubtful, but if its effect or signification is not, the conclusion will be the same
degree of probability as the existence of the cause or of the sign. That my friend is dead,
this is doubtful; the conclusion that I will draw from it, that he cannot write to me, will be
equally doubtful.

But when the existence & the effect of the cause are probables, or if it is the question
of signs, when the existence & the signification of the sign are only probables, then the
conclusion has only a composite probability. We suppose that the probability that my
friend has some affairs is \( \frac{3}{4} \) of certitude, & this that his affairs, if he has them, prevent him
writing to me is \( \frac{2}{3} \) of this certitude, then the probability that he will not write to me, will
be composed of two others, that which will be a half certitude.

3o We have indicated testimony as a third source of probability; & it keeps so closely
to the subject of which we give the principles, that one can dispense with reporting here
that which there is to say of it relative to the probabilities & to moral certainty. We are
not able to each see by ourselves: there are an infinity of things, often the most interesting,
on which it is necessary to be related to the testimony of others. It is therefore important
to determine, if it is not correct, at least in a manner which approaches it, the degree of
agreement which we can give to this testimony, & which is for us the probability of it.

When one tells us a tale, or when one advances a proposition of a number of those which
are substantiated by testimony, one must first examine the nature itself of the thing, & next
weigh the authority of the testimony. If, on all sides, we find that it lacks no conditions
requisite for the truth of the proposition, we can not refuse it ts consent; if it is evident that
it lacks one or many of these conditions, one must not hold undecided to reject it; finally, if
one sees clearly the existence of some of these conditions, & if we remain uncertain on the
others, the proposition will be probable, & so much more probable, as a greater number of
these conditions will hold.
As for the nature of the thing, the sole requisite condition, is that it be possible, that is to say, that there is nothing in its nature which forbids its existence, & nothing consequently which must prevent me from believing as soon as it will be sufficiently proved by an exterior proof, such as is that of testimony. To the contrary, if the thing is impossible, if it has in itself an invincible repugnance to exist, to some degree of credibility which can rise besides the proofs of the testimony, or other reasons extrinsic to its existence, I cannot believe it. Would someone claim to advance a contradiction, an absolute impossibility, would he join all sorts of proofs, he will never come in the end to persuade me that which is metaphysically impossible. A squared circle can be neither understood nor accommodated. Is the question a physical impossibility? let us be a little less difficult; we know that God has established himself the laws of nature, that he is constant in the observation of these laws; thus the mind repels to believe that they can be violated. However we know also that the one who has established them has the power to suspend them; that they are not an absolute necessity, but solely of convenience. Thus we ought not absolutely refuse our trust in testimonies or in the exterior proofs to the contrary; but it is necessary that these proofs be quite evident, in great number, & dressed in all the characters necessary in order to give our consent. Is it a question of moral impossibility or of an opposition to the moral qualities of intelligent beings? Although quite less delicate on the proofs or the testimonies which wish to persuade us, however it is necessary that we see this credibility which is found in the same characters, & in the effects which result from them; it is necessary that the actions follow naturally from principles which ordinarily produce them: it is thus that it seems impossible that a wise man, of a grave & modest character, is carried without reason, without motive to commit an indecency in public. On the contrary, an ordinary morally possible fact, conformed to the regular course of nature, persuades easily; it carries already to itself many degrees of probability; if the testimony adds to it in the least, it would become very probable. This probability will increase yet by the accord of a truth with others already known & established; if the story which one makes to us is so well linked with history, that one would not be able to deny it without reversing a sequence of well established historical facts, by that itself it is proven; if to the contrary it cannot find its place in history without deranging certain grand known events, by that even this story is rejected. Why is the history of the Greeks & Romans regarded among us as much more credible that that of the Chinese? It is that it leaves us an infinity of monuments of each kind which have a relation so necessary, or at least so natural with this history, & that links it such to general history, that they multiply the proofs of it to infinity; instead that of the Chinese has only little of the liaisons with the sequence of this general history which is known to us.

When one has weighed the proofs which are drawn from the nature itself of the thing, that one has recognized the possibility, & in some manner the degree of intrinsic probability, it is necessary to come to the validity itself of the testimony. It depends on two things; on the number of testimonies, & on the confidence which one can have in each of them.

For this which is of the number of testimonies, there is no person who does not sense that their testimony is so much more probable, as they are in so much greater number: one would believe likewise that it increases in probability in the same proportion as the number grows; so that two testimonies of an equal confidence would give a probability double of that of one, but one would be deceived. Probability grows with the number of testimonies in a different proportion. If one supposes that the first testimony gives me a probability which is carried to the \( \frac{9}{10} \) of certitude, the second, which I suppose equally believable, would it add to the probability of the first \( \frac{9}{10} \)? no, because then their two
reunited testimonies would make \( \frac{18}{10} \) of certitude, or a certitude & \( \frac{8}{10} \) more, this which is impossible. I say therefore that this second testimony will increase the probability of the first by \( \frac{9}{10} \) on that which remains to go to certitude, & will grow thus the reunited probability to \( \frac{99}{100} \), that a third will carry it to \( \frac{999}{1000} \), a fourth to \( \frac{9999}{10000} \), thus in sequence, approaching always more to certitude, without ever arriving entirely there: that which must not surprise, since whatever number of testimonies as one supposes, there must always remain the possibility of the contrary, or some degrees of probability quite small to the truth, that they are mistaken; here is the proof of it. When two testimonies say to me a thing, it is necessary, in order that I am mistaken by adding faith to their testimony, the one & the other induces me to error; if I am sure of one of the two, it matters little that the other be believable. Now, the probability that one & the other deceive me, is a probability composed of two probabilities, that the first deceives, & the second deceives. That of the first is \( \frac{1}{10} \) (since the probability that the thing is conformed in its relation is \( \frac{9}{10} \)); the probability that the second deceives me also is again \( \frac{1}{10} \): therefore the composite probability is the tenth of the tenth of \( \frac{1}{10} \); therefore the probability of the contrary, that is to say that which one or the other say truly, is \( \frac{99}{100} \). One sees that I myself represent here moral certitude as the term of a race course that the diverse testimonies which come to support it the one & the other, make me traverse. The first approaches me from a space, which has with all the license the same proportion as the force of his testimony has with the entire certitude. If his relation produces to me \( \frac{9}{10} \) of certitude, this first testimony will make me \( \frac{9}{10} \) of the track. Comes the second testimony as believable as the first; it advances me on the remaining path, precisely as much as the first had advanced me on the total space: the one had brought me forth to \( \frac{9}{10} \) of the course, the second approaches me again of \( \frac{9}{10} \) of the remaining tenth; so that with these two testimonies I have made \( \frac{99}{100} \) of all. A third of the same weight makes me travel through again \( \frac{9}{10} \) of the remaining hundredth, between certitude & the point where I am; there will remain no more than the thousandth, & I will have made \( \frac{999}{1000} \) of the course, & thus in sequence.

This method to calculate the probability of the testimony, is the same for a number of testimonies of which the credibility is different; that which, for the ordinary, is more conformed to the nature of things. Let a fact be rendered to me by three testimonies; the relation of the first is equivalent to \( \frac{5}{6} \) of certitude; the second produces to me as \( \frac{2}{3} \); & the third less believable than the two others, will give to me only a \( \frac{1}{2} \) certitude if it were alone. Then, supposing always that I have no reason to suppose some concert among them, I say that their reunited testimony gives to me a probability that is \( \frac{35}{36} \) of certitude, because the first advances me \( \frac{5}{6} \), there remains \( \frac{1}{6} \), of which the second will make me travel through \( \frac{2}{3} \); thus there will be again \( \frac{1}{2} \) of \( \frac{1}{6} \), which is \( \frac{1}{12} \); & the third advancing me \( \frac{1}{2} \), I am no more extended from the end of the racecourse than \( \frac{1}{36} \): I would have therefore traveled through \( \frac{35}{36} \); besides it is indifferent in which order one takes them, the result is the same.

2° This principle can suffice for all the calculations on the value of testimony. As for the faith that each testimony merits, it is based on its capacity & on its integrity. By the first, it can not be deceived; by the second, it seeks not to deceive me; two equally necessary conditions; the one without the other does not suffice. Whence it follows that the probability that gives birth to the relation of a testimony in which we recognize this capacity & this integrity, must be regarded & calculated as a composite probability. A man comes to me to say that I have the big prize; I know him to be not too intelligent; he is able to be deceived: all counted, I evaluate the probability of his capacity at \( \frac{8}{9} \); but perhaps he
takes pleasure in deceiving me. We pose that there are odds of 15 against 1 that he is of
good faith, the probability of his integrity will be therefore $\frac{15}{16}$. I say that the assurance of
his testimony or the composite probability of his capacity, & of his integrity, will be $\frac{5}{6}$ of
$\frac{15}{16}$, that is to say $\frac{5}{6}$ of certitude.

The surest manner to judge the capacity & integrity of a testimony, would be experience. It
would be necessary to know exactly how often this same man has deceived or has said the
truth; but this experience is limited, & wanted for the ordinary. Instead one has recourse to
the public & particular rumors, to the exterior circumstances where the testimony is found.
Has he received a good education? is he of a rank which is supposed to engage him to
respect further the truth? is he of an age which gives more weight to his testimony? is
he disinterested in this? or what can be his end? extract some advantage from it, or shun
thence some pain? his taste, his passion are they flattered to deceive us? is this a sequence
of prevention, of hatred? Quite as much of circumstances which it is necessary to examine
if we have not experience, & of which it is quite difficult to determine the correct value.

Moreover, the capacity of a testimony supposes, beyond the well-conditioned sense, a
certain firmness of the mind which allows oneself neither frightened by danger, nor sur-
prised by novelty, nor seduced by a judgment too rash. It is more believable in proportion
as the thing of which he speaks to us is more familiar & more known to him; his story itself
makes often a proof of his capacity, & announces to me that he has taken or ignored all
the necessary precautions in order to not deceive himself: the more he has reiterated them,
the more he has the right to my confidence. This capacity to understand well depends yet
on the attention to observe, on the memory, on the time: other conditions which, joined
in the manner to relate clearly & in detail, influences on the degree of probability which a
testimony merits.

One must not ignore the silence of those who would have interest to contradict a tes-
timony, if at least he is extorted neither by fear, nor by authority. It is difficult indeed to
estimate the weight of a similar negative testimony; one can assure in general that the one
who makes simply only to be quiet, merits less attention than the one who assures a fact.
If nonetheless the fact is such that he has been able to ignore it, if he would have served to
evaluate the rest of his story, if he would have been interested in the relation, or if his duty
would call it; in a similar case, it is certain that his silence is worth a testimony, or at least
it reduces & diminishes the probability of the opposing testimony.

We must still say a word on the testimonies by hearsay, or on the diminishing of tes-
timony which, passing from mouth to mouth, they arrive to us only by way of a chain of
testimony. It is clear that hearsay testimony, all things equal besides, is less believable than
an eyewitness testimony; because if the one is deceived, or has wish to deceive, the hearsay
testimony which follows it, however faithful, will report to us only an error; & even then
the first would have debited the truth, if the hearsay testimony is not faithful, if it is wrong
intended, if he has forgotten or confounded some essential part of the story, if he mixes
with his own, he no longer reports the pure truth to us; thus, the confidence that we owe
to this second testimony, is reduced already, will be reduced in measure as it will pass by
more mouths, in measure as the chain of testimony will be extended. It is easy to calculate
on the established principles, the value of this probability.

We follow the example of which we have made use. Pierre announces to me that I have
had a lot of one thousand livres: I estimate his testimony to $\frac{9}{10}$ of certitude, that is to say
that I will give my expectation only for 900 francs. But Pierre says to me that he knows
it from Jacques; now, if Jacques would have said to me, I would have estimated his report
to $\frac{9}{10}$ by supposing it as believable as Pierre; thus me who am not entirely sure that Pierre
is not deceived in receiving this testimony of Jacques, or that he has not some design to
deceive me, I must count only \( \frac{9}{10} \) of 900 livres, or on \( \frac{9}{10} \) of \( \frac{9}{10} \) of 1000 livres, that which makes 810 livres. If Jacques would hold the fact of another, I would take again on this last
assurance \( \frac{9}{10} \), supposing this third equally believable, & my expectation would be reduced
to \( \frac{9}{10} \) of \( \frac{9}{10} \) of \( \frac{9}{10} \) of 1000 livres, or 729 livres, & thus in sequence.

Who will wish to take the pain to calculate on this method, will find that, if the confi-
dence that one must have in each testimony is of \( \frac{95}{100} \), the thirteenth testimony will transmit
no more than \( \frac{1}{2} \) certitude, & then the thing will cease to be probable, or there will not be
more extrinsic reason to believe it, than to not believe it. If the probability due to each tes-
timony is \( \frac{99}{100} \), it will be reduced to \( \frac{1}{2} \) certitude only when the testimony will have passed
by seventy mouths; & if this confidence were suppose of \( \frac{999}{1000} \), it would be necessary a
chain of 700 testimonies in order to render the fact uncertain.

These long enough calculations can be shortened by this general rule, of which the
simple algebra furnishes us the result & the demonstration. Take \( \frac{7}{10} \) of the quotient of the
division of the probability of a simple testimony by the contrary probability, as here of \( \frac{95}{100} \)
by \( \frac{5}{100} \), or of 95 by 5, which is 19, of which I take \( \frac{9}{10} \), & you will have the testimony which
leaves you in a half-certitude; in this example this is \( 13 \frac{3}{10} \), that which gives the thirteenth
testimony.

It will be likewise if the successive testimonies are supposed of unequal force; whence
there is place to conclude in general, that it is necessary to make little basis on hearsay,
without leaving to go however to historic Pyrrhonism, since here one can reunite the prob-
babilities that give many collateral chains of successive testimonies. We suppose that a fact
arrives to us by a simple succession of testimonies by word of mouth, in a manner that each
testimony succeeds to the other at the end of twenty years, & that the confidence in each
testimony diminishes by \( \frac{9}{10} \); by the preceding rule, at the end of twelve successions, or of
240 years, the fact would become uncertain, being proved only by these 12 testimonies;
but, if this chain of testimonies is fortified by nine other similar chains which combine to
attest to the same truth, then there will be more than one thousand against one in favor
of the fact; if one supposes one hundred chains of testimony, there will be more than two
million against one in favor of the fact.

If the testimony is transmitted by writing, the probability increases infinitely, as long
as it subsists & is conserved a quite long time; the concurrent testimony of many copies
or printed books which form as many different chains, give a probability so great as it
approaches indefinitely certitude; because to suppose that each copy can endure 100 years,
that which is the less, & if at the end of this time the authority, not of a single copy, but of
all those which have been made on the same original, is alone \( \frac{99}{100} \), then it will be necessary
more than seventy successions of 100 years, or 7000 years in order that the fact become
uncertain; & if one supposes many chains of testimonies, which combine all to attest the
same fact, the probability increases so much, that it becomes infinitely little different from
entire certitude, & will surpass by much the assurance which one could have of the mouth
of one or even of many eyewitness testimonies. There are other circumstances which it is
easy to suppose & which demonstrate the great superiority of the written tradition over the
oral tradition.

We have indicated two other sources of probability, analogy & hypotheses on which we
refer to the articles INDUCTION, ANALOGY, HYPOTHESIS, SUPPOSITION. These
principles can suffice to explicate all the theory of probability. We have given only the
elements; one will find the application of it in all the good works, which are in great
number on this subject. Such are the Essais sur les probabilités de la vie humaine, by Mr.
Deparcieu; l’Analyse des jeux de hasard, by Mr. de Montmort, who gives the theory of combinations, for example the article of this Dictionary under this word, & many others which have relation, especially the Ars Conjectandi, of Mr. Jacques Bernoulli, & some Memoirs of Mr. Halley, which are found in the transactions of England⁴, n. 196 & the following, which all serve to determine the possibility of the events, & the degrees by which we arrive to moral certitude.

We conclude that it would not be entirely impossible to reduce all this theory of probabilities to a sufficiently regular calculus, if good geniuses would wish to combine by the researches, some observations, a follow-up study, & an analysis of the heart & of the mind, based on experience, to cultivate this branch so important of our knowledge, & so useful in the continual practice of life. We agree that there is yet more to make, but the consideration of this which is lacking must excite to fill these voids, & the importance of the object offers of what to compensate amply some difficulties.

⁴Philosophical Transactions of the Royal Society.